THEORETICAL STUDIES OF THE IDENTITY ALLYL TRANSFER REACTIONS^{*}

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Ab initio studies on the S_N^2 identity exchange reactions $RCH_2X + X^- \rightarrow X^- + RCH_2X$ for $R = CH_2CH$ with $X^- = H$, NH_2 , OH, F, PH_2 , SH and Cl, and for $R = CH_3$ and CH = C with $X^- = Cl$ were carried out at the HF and MP2 levels using the $6-31++G^{**}$ basis sets. The activation barriers, ΔE^* , and major structural changes, $\Delta d^+(C-X)$, in the activation process are closely related to the electronegativity of the R and X groups. The effect of electronegativity is twofold: a stronger electronegativity of R and/or X leads to a lesser electronic as well as structural reorganization required in the activation and to a greater correlation energy in the transition state. The former effect lowers the energy barriers at both the HF and MP2 levels whereas the latter lowers only the correlated (MP2) activation energies. Results with $R = CH_2CH$, as a model for $R = C_6H_5$, indicate that 'benzylic effect' arises mainly from the relatively stronger electron acceptor ability of the phenyl group.

INTRODUCTION

Bimolecular nucleophilic substitution reactions at carbon have been extensively studied experimentally and theoretically. Recently, much work has focused on the gas-phase reactions in order to clarify intrinsic features of S_N2 processes. In this respect, gas-phase identity exchange reactions, in which the nucleophile and leaving group are the same, have attracted considerable attention from experimentalists² and theoreticians.³

Theoretical studies of gas-phase identity exchange reactions have played an essential role in providing evidence for a double-well potential energy surface (PES) and in establishing usefulness of the Marcus equation⁴ by showing remarkably good agreement between intrinsic barriers calculated MO theoretically and those derived from the Marcus equation.^{3a-c,3i}

Most of these theoretical studies have, however, involved methyl transfer reactions, R = H in the equation (1)

$$X^{-} + RCH_2 X \rightleftharpoons XCH_2 R + X^{-}$$
(1)

In a series of theoretical studies on methyl transfer reactions, Shi and Boyd^{3h,i} stressed the importance of including diffuse functions in the basis set and incorporating electron correlation effects in the calculation. They showed that the intrinsic barrier is related to the electronegativity of the leaving group, X^- ; as the

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CCC 0894-3230/95/070473-11 © 1995 by John Wiley & Sons, Ltd. electronegativity of the leaving group increases, the intrinsic barrier decreases. Recently, Wladkowski *et al.*^{3j} reported a comprehensive study on the S_N^2 identity exchange reaction involving acetonitrile group transfer, R = CN in equation (1). They concluded that the effect of CN substitution on the stability of the S_N^2 transition state (TS) does not arise from 'resonance' effects in the TS.

Delocalization of π or lone-pair electrons of the nucleophile into the substrate benzene ring in the S_N^2 reactions of the benzyl derivatives is known to stabilize the TS, I, and results in a rate enhancement.⁵ This 'benzylic effect' causes bond contraction of the $C^{\alpha}-C^{\beta}$ bond.



To extend our understanding of the factors that are important in controlling the intrinsic reactivities, we have carried out *ab initio* MO calculations on the identity allyl transfer reactions, $R = CH_2CH$ in equation (1), with X = H,

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NH₂, OH, F, PH₂, SH and Cl. We have also investigated the effect of α -substitution on the reactivity by including R = CH₁ and HC =C in equation (1) for X = Cl.

COMPUTATIONAL METHOD

The 6–31G extended basis sets with diffuse functions and polarization functions $(6-31++G^{**})^7$ were used throughout. To account for the electron correlation, second-order Møller–Plesset perturbation theory (MP2) was adopted. The MP2 calculations are known to give size-consistent results, which is an important requirement for the study of chemical reactivity. We kept the same level of computation in the energy calculation as that used in geometry optimization. Unless noted otherwise, two types of results are reported: HF (HF/6–31++G^{**})/HF/6–31++G^{**}) and MP2 (MP2/6–31++G^{**}//MP2/6–31++G^{**}).⁷ In order to examine the effects of diffuse and polarization functions on the calculated geometries, $6-31+G^*$ (and $6-31++G^*$) level⁷ computations were also performed for X = H, F and Cl.

Geometries were optimized using analytical energy gradient methods at the HF and MP2 levels. The geometries of reactants and TSs were fully optimized with C_{s} symmetry constraint for the latter, and all positive and only one negative eigenvalues, respectively, in the Hessian matrix were identified to confirm the equilibrium and transition states⁸ in all the HF level calculations. For X = F, an additional very low negative frequency (57.0i cm⁻¹) was obtained but this was found to reduce further at the MP2 level (24.9i cm⁻¹). The transition vector for this low imaginary frequency was found to correspond to a weak bending mode. As Wu and Houk⁹ have pointed out, low imaginary frequencies can occur due to bending in addition to rotation on very flat potential surfaces. (We have calculated the TS structure under C_1 symmetry constraint with full geometry optimization and arrived at a structure in which $\check{C}^1 C^2 C^3 \check{F}_2$ heavy atoms are coplanar with two hydrogens on C³ perpendicular to this plane. This TS structure had only one negative eigenvalue (640.5i cm⁻¹), 1.8 kcal mol⁻¹ lower at the HF level but higher by 0.3 kcal mol⁻¹ at the MP2 level than the energies at the corresponding levels under C_s symmetry constraint, indicating that the potential is very flat around the TS.) Population analyses were performed by natural bond orbitals (NBO) method.¹⁰ Geometries of reactant (ion-molecule) complexes corresponding to backside attack were fully optimized. All calculations were carried out using the Gaussian 90 and 92 program.¹¹

RESULTS AND DISCUSSION

Geometries

Optimized geometries of substrates (S), ion-molecule complexes (C) and transition states (TS) at the HF and MP2 levels are summarized in Table 1. The data reveal

that in general the HF results give shorter bond distances in the substrate molecule than the MP2 results. For X = H, however, both the HF and MP2 results give bond lengths which are very close to the experimental results (within ± 0.003 Å), except for $d(C^1-C^2)^{12}$ [experimental bond lengths are $d(C^{1}0C^{2}) = 1.318$ and $d(C^2 0 C^3) = 1.501$ Å]; the MP2 level overestimates this length by 0.02 Å. In all cases, bond length changes along reaction coordinate $(S \rightarrow C \rightarrow TS)$ are significant for $d(C^2-C^3)$, $d(C^3-X^{6,7})$ and $d(C^3-H^{4,5})$; for $d(C^2-C^3)$, $d(C^3-X^{6,7})$ and $d(C^3-H^{4,5})$; $d(C^3-H^{4,5})$ is lengthened in the ion-molecule complex whereas it is shortened again in the TS. The important bond length changes are, however, those of $d(C^2-C^3)$ and $d(C^3-X^{6.7})$ involved in the activation, i.e. $\Delta d^*(S \rightarrow TS)$ values. The basis set dependence of these two bond lengths is summarized in Table 2 for X = H, Fand Cl. Examination of Table 2 indicates that the most significant structural change in the activation process is the extension of C^3-X since the decrease in the C^2-C^3 distance $[\Delta d^*(C^2-C^3)]$ is very small compared with the increase in the C^3-X^6 distance $[\Delta d^*(C^3-X^6)]$. The extension of the double bond, $\Delta d^*(C^1-C^2)$, is less than 1% in all cases and hence is negligible. Inclusion of electron correlation generally shortens further the distances of the two bonds. Additions of polarization and diffuse functions lead very small changes in the HF level bond lengths. By far the greater changes are accompanied by inclusion of the electron correlation effect; nearly a 10% bond length decrease is effected by the inclusion of electron correlation with the $6-31++G^{**}$ basis set. For heavy-atom Xs (X = F and Cl), the percentage changes in $\Delta d^*(C^3-X^6)$ value are smaller than those for X = H and also the effects of adding polarization and diffuse functions in addition to including electron correlation are much smaller than those for X = H.

The angle $a(C^1C^2C^3)$ deviates slightly from 120° in all three structures, S, C and TS, with the MP2 result giving the nearest value to 120°. Angles $a(C^2C^3X^6)$ and $D(C^1C^2C^3X^6)$ approach 90° at the TS, but here again the MP2 values are the nearest to 90°. Since a C_s symmetry constraint is applied to the TS, the angle $D(C^1C^2C^3H^4)$ is 0°.

Energy barriers

Two types of energy barriers, the activation energy, ΔE^* , and the intrinsic barrier, $E_{0,1}^*$ in Figure 1, were determined and summarized in Table 3. We note that inclusion of electron correlation tends to reduce both the activation barrier and the intrinsic barrier. The energy barriers, ΔE^* and $E_{0,1}^*$ for the identity exchange reactions separate into three groups depending on the row of the Periodic Table; X = H alone belongs to the first group, $X = NH_2$, OH and F to the second and $X = PH_2$, SH and Cl to the third. Similar classification of X into separate groups were reported for the ΔE_0^* Table 1. Optimized geometries of substrates (S), ion-molecule complexes (C) and transition state (TS) at the HF and MP2 levels

 $H^{0}_{H^{0}} C^{1} = C^{2}_{H^{10}} C^{3}_{H^{0}} X^{0} + (X^{7})^{-}_{H^{0}}$

			В	ond lengths (Å)	Bond a	ngles (°)	Dihedral a	ingles (°)
x	Species	Level	$d(C^2-C^3)$	$d(C^3-X^6)$	$d(C^3-H^4)$	$a(C^2C^3X^6)$	$a(C^2C^3)H^4)$	$D(C^1C^2C^3X^6)$	$D(C^{1}C^{2}C^{3}H^{4})$
н	S	HF	1.5025	1.0869	1.0845	110.76	111.42	120.62	0.00
		MP2	1-4989	1.0914	1.0899	110.99	110.93	120.46	0.00
	С	HF	1.5002	1.0858	1.0876	109.95	111.96	121.63	0.05
		MP2	1.3982	1.0916	1.0930	110.20	111.81	121.46	0.07
	TS	HF	1.4811	1.6702	1.0630	92.31	121.12	91.88	0.00
		MP2	1.4781	1.5712	1.0741	89.98	121.36	91.30	0.00
NH_2	S	HF	1.5039	1.4578	1.0842	110.78	109-43	124.75	5.50
-		MP2	1.4988	1.4710	1.0912	110-13	109-26	120.71	2.40
	С	HF	1.5069	1.4491	1.0838	111.81	109.65	131.09	10.92
		MP2	1.5001	1.4636	1.0912	111.62	109.60	123.58	4.33
	TS	HF	1.4767	2.0422	1.0632	92.07	119.86	94.20	0.00
		MP2	1.4638	2.0181	1.0783	91.11	119-59	94.11	0.00
OH	S	HF	1.4991	1.4066	1.0871	108-29	110.13	128-24	6.74
		MP2	1.4934	1.4369	1.0946	107-46	109.95	122.82	1.99
	С	HF	1.5114	1.4261	1.0814	111.26	111.12	186.57	48.62
		MP2	1.5051	1.4568	1.0888	111.14	111.32	191.36	42.82
	TS	HF	1.4779	1.9556	1.0611	92.41	119.79	91.31	0.00
		MP2	1.4661	1.9425	1.0736	91.36	119.65	90.75	0.00
F	S	HF	1.4959	1.3797	1.0819	109.64	111.68	125.53	6.21
		MP2	1.4903	1.4170	1.0899	109-45	111.57	120.80	2.27
	С	HF	1.4957	1.4052	1.0843	107.67	111.05	121.32	5.41
		MP2	1.4880	1.4447	1.0923	107.51	110.93	120.42	5.40
	TS	HF	1.4798	1.8605	1.0619	93.91	119.88	91.79	0.00
		MP2	1.4710	1.8467	1.0739	93.11	119.59	91.46	0.00
PH,	S	HF	1.5029	1.8752	1.0797	111.64	110-18	110-11	-9.00
-		MP2	1.4970	1.8759	1.0917	110.52	109.75	108.90	-9.80
	С	HF	1.5011	1.8725	1.0866	111.41	110.66	105.01	-14.38
		MP2	1.4933	1.8727	1.0934	109.92	110.52	106-44	-13.17
	TS	HF	1.4702	2.6079	1.0638	94-83	121.09	91.38	0.00
		MP2	1.4579	2.5099	1.0760	91.28	121.15	90.76	0.00
SH	S	HF	1.5007	1.8338	1.0814	109-61	110.71	115.76	-5.25
		MP2	1.4952	1.8314	1.0895	108-89	110.08	113.70	-7.37
	С	HF	1.4996	1.8347	1.0783	111.72	111.92	134-40	9.21
		MP2	1.4950	1.8309	1.0865	112-35	111.13	137.43	12.94
	TS	HF	1.4693	2.5349	1.0625	95.75	120.54	91-94	0.00
		MP2	1.4633	2.4111	1.0729	92.86	120.22	91.99	0.00
Cl	S	HF	1.4954	1.8045	1.0787	111-25	111.84	119.74	-0.50
		MP2	1.4902	1.7971	1.0878	111.15	110.92	117.62	-1.81
	С	HF	1.4928	1.8282	1.0782	110-15	112-11	112.57	-4-65
		MP2	1.4869	1.8123	1.0884	110.23	111-18	111-95	-5.89
	TS	HF	1.4618	2.4991	1.0642	98.89	120.59	92.43	0.00
		MP2	1.4604	2.3625	1.0733	96.05	120.00	92.65	0.00

values of identity methyl transfer reactions by Shi and Boyd.³ⁱ They attributed this grouping to the type of hybridization and the electronic structure of the TS. No doubt periodicity of homonuclear single covalent bond energies of the heavy-atom elements in X plays an important role for this grouping, since the bond energies of the two corresponding first- and second-row elements differ uniformly by ca 20 kcal mol⁻¹ (1 kcal = 4.184 kJ).¹² Within each group, the ΔE^* and ΔE^*_0 values, at both the HF and MP2 levels, vary linearly with electronegativity (χ) (the theoretical values are generally in good agreement with those for X

X	Basis set	Species	$d(\mathrm{C}^{1}-\mathrm{C}^{2})$	$d(\mathrm{C}^2\mathrm{-}\mathrm{C}^3)$	$d(C^3-X)$
Н	HF/6-31+G*	GS	1.3223	1.5029	1.0868
	·	TS	1.3277	1.4775	1.6898
		Δd^*	+0.0054	$-0.0254 (-1.7)^{a}$	$+0.6030 (+55.5)^{a}$
	$MP2/6-31+G^*$	GS	1.3400	1.4989	1.0954
		TS	1.3461	1.4689	1.6367
		Δd^*	+0.0061	-0.0300 (-2.0)	+0.5413 (+49.4)
	$HF/6-31++G^{**}$	GS	1.3222	1.5025	1.0869
	,	TS	1.3263	1.4811	1.6702
		Δd^*	+0.0041	-0.0214(-1.4)	+0.5833 (+53.7)
	$MP2/6-31+G^{**}$	GS	1.3396	1.4971	1.0902
	1	TS	1.3435	1.4763	1.5707
		Δd^*	+0.0039	-0.0208(-1.4)	+0.4805(+44.1)
F	$HF/6-31+G^{*}$	GS	1.3208	1.4962	1.3789
		TS	1.3197	1.4802	1.8589
		Δd^*	-0.0011	-0.0160(-1.1)	+0.4800(+34.8)
	$MP2/6-31+G^*$	GS	1.3398	1.4891	1.4178
	,	TS	1.3419	1.4699	1.8497
		Δd^*	+0.0021	-0.0192 (-1.3)	+0.4319 (+30.5)
	$HF/6-31++G^{**}$	GS	1.3207	1 4959	1.3797
		TS	1.3196	1.4798	1.8605
		Δd^*	-0.0011	-0.0161(-1.1)	+0.4808(+34.8)
	$MP2/6-31 + +G^{**}$	GS	1.3391	1.4886	1.4156
	,	TS	1.3412	1.4689	1.8457
		Δd^*	+0.0021	-0.0197 (-1.3)	+0.4301(+30.4)
Cl	$HF/6-31+G^{*}$	GS	1.3210	1.4957	1.8040
		TS	1.3214	1.4623	2.4966
		Δd^*	+0.0004	-0.0334 (-2.2)	+0.6926 (+38.4)
	$HF/6-31 + +G^{**}$	GS	1.3208	1.4954	1.8045
		TS	1.3214	1.4618	2.4991
		Δd^*	+0.0006	-0.0336 (-2.3)	+0.6946 (+38.5)
	$MP2/6-31 + +G^{**}$	GS	1.3391	1.4887	1.7-91-952
		TS	1.3430	1.4585	2.3600
		Δd^*	+0.0039	-0.0302 (-2.0)	+0.5648 (+31.5)

Table 2. Basis set dependence of bond lengths (Å)

^a Values in parentheses are percentage changes: $(\Delta d^*/d^0) \times 100$.



C : Ion-Molecule Complex, (X ---- RCH₂X).

- TS : Transition State, (X RCH₂ X)⁻.

Figure 1. Two types of energy barriers, the activation energy, ΔE^* , and the intrinsic barrier, ΔE_0^* , of the gas-phase identity exchange reaction in equation (1)

	HI	7	MP2	2	
х	ΔE_0^*	Δ <i>E</i> **	ΔE_0^* ,	ΔE^*	χ,
н	67.07	61.83	55.13	49.90	_
NH ₂	56.66	40.04	43.34	24.79	6.16
OH	(40-11)°	28.58	(27·88)°	14.66	6.95
F	22.96	8.82	14.98	-0.29	10.01
PH,	44.87	38.63	33-26	22.54	5.05
SH	(30·11)°	23.52	(24.92)°	14.78	5.69
Cl	16-82	8.30	18.80	8.11	7.65

Table 3. Energies (kcal mol⁻¹) calculated at the HF and MP2 levels for reactions $CH_2CHCH_2X + X^{-1}$

*Corrected for zero-point energies.

^b Group electronegativities calculated at the CI(SD) level.¹³ ^c Ion-molecule complex energy under backside attacking constraint for

Х-

radicals¹⁴) of the X group (Figures 2 and 3). The activation barrier, ΔE^* , and intrinsic barrier, ΔE_0^* , are lowered by increasing the electronegativity or alternatively the electron affinity of X in each group. A similar trend was noted by Shi and Boyd³ⁱ for the intrinsic barrier, ΔE_0^* in the identity exchange reactions involving methyl transfer [R = H in equation (1)]. Inspection of Table 3 indicates that for the allyl transfer reactions an

approximate linearity holds between the two types of energy barriers, ΔE^* and ΔE_0^* , within each group.

Table 4 gives the changes involved in the activation process, i.e. $S \rightarrow TS$, in bond distances for $d(C^2-C^3)$ and $d(C^3-X)$ at both the HF and MP2 levels and atomic charges for C³ and X at the MP2 level. There are systematic changes within each group: the percentage changes $(\Delta d^*/d^0 \times 100)$ in $d(C^2-C^3)$ and $d(C^3-X)$ become smaller with increasing electronegativity. This means that within each group or within a row of the Periodic Table, the stronger the electronegativity of X, the smaller is the extent of structural changes involved in the activation process, and the smaller is the activation barrier. This is consistent with the results of Mitchell et al.,¹⁵ who defined the percentage change as the distortion index (DI) and showed that DI reflects 'tightness' or 'looseness' of the TS and ΔE_0^* , for identity methyl transfer increases as DI increases or as the electronegativity of X decreases. The intrinsic barriers are found to be linearly correlated with the total deformation energies, which in turn are dominated by the C-X stretching, i.e. DI, and are related to the experimental C-X bond dissociation energies.

Again, within each group, the stronger the electronegativity of X, the smaller is the amount of charge transferred to the reaction centre carbon from the



Figure 2. Plots of activation energy (ΔE^*) versus electronegativity (χ)



Figure 3. Plots of intrinsic barrier (ΔE_0^*) versus electronegativity (χ)

nucleophile $X^{-}[\Delta q^{*}(C^{3})]$ and to the leaving group X $[\Delta q^{*}(X)]$.

The correlation part of the electronic energy in the S_N^2 process is known to change significantly when going along the reaction path from reactants to TS owing to substantial electronic charge redistribution and the formation of a formally penta-coordinated reaction centre carbon atom.^{3g} According to the valence bond configuration mixing (VBCM) model of Pross and coworkers, ^{16a-c} the TS occurs approximately at the crossing point of the reactant (structure III) and product VB structures (not shown), and the confidence is affected by contributions from other VB structures, e.g.IV and V. For a more electronegative X, the contribution of valence bond configuration^{3i,16d-f} IV to the TS can be greater since a smaller extent of structural and electronic charge reorganization is required.



Comparison of energy barriers for X = F and Cl indicates that the electron correlation effect is especially large for X = F. The two barriers, ΔE^* and ΔE_0^* , are higher for X = F at the HF level, but in contrast they are lower for X = F than for X = Cl at the MP2 level. These reversals in the order of activation barriers for X = F and Cl with lower correlated barriers for X = F are also found for the identity methyl (R = H) transfer reactions (Table 5), which is in agreement with the experimental activation barriers, $\Delta E_0^{\pm 2g,3g}$ This trend is mainly due to a great lowering of the correlated barriers for X = F by inclusion of electron correlation; for X = F, ΔE_0^* and ΔE^* are lowered by ca 8 and 10 kcal mol⁻¹, respectively, whereas for X = Cl, ΔE_0^* is raised by 2 kcal mol⁻¹ and ΔE^* is lowered by only less than 1 kcal mol^{-1} by inclusion of electron correlation. Similar trends have been reported for the identity methyl³ⁱ and acetonitrile group^{3j} transfers. Table 5 compares the electron correlation effect on the energy barriers for the two identity exchange reactions. It can be seen that in the methyl transfer reactions, energy barriers are lowered for X = F but they are raised for X = Cl by including electron correlation. In contrast, however, the energy barriers are lowered for X = Cl in the acetonitrile group transfer reaction. Hence the effect of electron correlation on the energy barriers depends on the nature of both the R and X groups. One common feature to the methyl and allyl transfer reactions is that the electron correlation effect is

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	ŀ	iF		MP2		
x	$\Delta d^{*}(C^{2}-C^{3})$ (%)	$\Delta d^{*}(C^{3}-X)$ (%)	$\Delta d^{*}(C^{2}-C^{3})(\%)$	$\Delta d^{*}(\mathrm{C}^{3}\mathrm{-X})(\%)$	$\Delta q^{*}(\mathbf{X})$	$\Delta q(C^3)$
н	+1.4	+53.7	-1.4	+44-1	-0.605	-0.611
NH ₂	-1.8 -1.4	+40.1 +39.0	-2·3 -1·9	+37.2 +35.2	-0·468 -0·394	-0·367 -0·286
F	-1.1	+34.8	-1.3	+30.4	-0.319	-0.227
PH ₂	-2.2	+39.1	-2.6	+33.7	-0.791	-0.486
Cl	-2.1 -1.5	+38.2 +38.5	-2.0	+31.6 +31.5	-0.619	-0.385

Table 4. Changes $(S \rightarrow TS)$ in bond length $[\Delta d^*(\%) = (\Delta d^*/d^0) \times 100]$ and changes (Δq^*) in electronic units)^a for reactions $CH_2CHCH_2X + X$

Table 5. Electron correlation (EC) effects on energy barriers (kcal mol⁻¹) for identity exchange reactions of $RCH_2X + X^{-1}$ with R = H and CN

			ΔE_0^*	Δ	E [*]
R	x	HF	HF + (EC)	HF	HF + (EC)
н	F	20.0	17-1	7.4 (5.7)	$3.8 (-1.0)^{b}$ 8.9 (7.7) ^b
CN	Cl	22.1	11.4°	5·8	- 5 ·7

*Valence-shell double ζ (DZ) with diffuse functions (D) on X and polarization functions (P) on all atoms (DZDP). Electron correlation was accounted for by the CI(SD) approach.^{3g} ^b At the MP2/6-31++G^{**} level for the values in parentheses.^{3h} ^c At the MP2/6-31+G(2d,2p)//MP2/6-31+G(d,p) level.^{3j}

stronger for X = F than for Cl. As a result, the correlated energy barriers for F become smaller than those of Cl.

In order to examine the effects of the group R [in equation (1)] and of the electron correlation, relevant results are compared in Table 6 for the identity exchange reactions involving RCH₂Cl + Cl⁻ with various R. Some interesting effects of the group R (mostly unsaturated) emerge. (1) As the group electronegativity $(\chi)^{13}$ or electron-withdrawing power (as represented by Taft's polar substituent constants, σ^* , in aliphatic systems)¹⁷ of R increases, the activation barrier, ΔE^* , at the MP2 level decreases. A few gasphase experimental rate constants reported¹⁸ which are directly comparable to the results in Table 6 (for R = H, CH₃ and CN) are consistent with the trend in the activation barrier (ΔEFO_{MP}^*), except that there is an uncertainty in the reported rate constant for $R = CH_3$. However, experimental results for soft nucleophiles $(X = HS^{-} and Cl^{-})$ are in good agreement with our results for $X = Cl^-$ with R = H, CH_3 , CH_2CH and CN. (2) The HF energy barriers are lower than the MP2 barriers ($\Delta EFO_{HF}^* < \Delta EFO_{MP}^*$) for substrates with a weakly electronegative R, but this order of energy

barrier reverses to $\Delta EFO_{HF}^* > \Delta EFO_{MP}^*$ for substrates with a strongly electronegative R. (3) The percentage extension of $d(C^3-X)$ in the activation process tends to increase as the electronegativity of R decreases.

Now, if we compare the valence bond configurations IV and V with the reactant configuration, III, IV is certainly a more electron-localized structure with a greater hardness and V a more delocalized structure with less hardness than III.¹⁹ This means that electron correlation is greater in IV whereas it is smaller in V than in III.¹⁹ Hence a greater contribution of structure IV to the TS should result in a larger magnitude of electron correlation energy in the TS than in the reactant; in contrast, a greater contribution of structure V to the TS will result in a smaller magnitude of electron correlation energy in the TS than in the reactant substrate. The effects will be stronger the greater is the contribution of IV and V to the TS.

If the electron correlation energy in the TS is greater than that in the ground state (substrate), $\Delta E_{corr}^* > 0$, a net reduction of correlated energy barriers, ΔE_{MP}^{*} , will result; $\Delta E_{MP}^{*} = (E_{SCF}^{*} - E_{corr}^{*}) - (E_{SCF}^{0} - E_{corr}^{0}) = \Delta E_{HF}^{*} - \Delta E_{corr}^{*} (<\Delta E_{HF}^{*})$ (Figure 4). As the electronegativity of X^{-} and/or R increases, the contribution of the ionic valence bond configuration, IV, to the TS increases, and leads to the lowering of the correlated energy barriers,



Figure 4. The SCF and correlation energy levels in the ground state (GS) and transition state (TS)

					level 1	or reactions RCH ₂ Cl + C	31-					
	Ā	+0 50	A	E ⁴				FI	Q			
R	HF	MP2	HF	MP2	$d^{*}(\mathbb{C}^{3}-\mathbb{X})^{a}$	$\Delta d^{4}(\mathbf{C}^{3}-\mathbf{X}) \ (\%)^{\mathrm{b}}$	Ħ	, r	a	••	×	0 • ^d
H°	15.47	17-34	6.59	7.68	2.316	+30.2					1	0-49
CH,	18-47	22-20	9.04 40.6	11-04	2.361	+32.0					4.42	8 0
CH,=CH	16-82	18-80	9-02	8.12	2.360	+31.5(-2.0)	-0.3955	+0-2286	-0-8407	+0.3316	5.18	0-56
CH≣C	20-00	19-06	10-79	6-84	2-343	+30.7(-1.9)	-0.4115	+0.2986	-0-8523	+0.3229	8.21	2.18
N≡C	21-83 ⁶	17-21 ^f	5.70	-0.27	2.294	+29.0(-1.7)	-0-4893	+0.2795	-0-8899	+0.3044	8-63	3.30
*I enath of th	ν. Γ ³ _ Υ ΗΛΠ	d at the TS										İ

Table 6. Energies (kcal mol⁻¹) calculated at the HF and MP2 levels and changes in bond length $[\Delta d^{4}(C^{3}-X) \text{ in } \mathring{A}]$ and FMO energy level (in hartree) at the MP2

- Length of the C⁻⁻ X bond at the 1S. - Concentage change (S \rightarrow Y) in $d(C^3 - X)$: $(\Delta d^3/d^0) \times 100$. The values in parentheses are the $\Delta d^4(C^3 - C^2)$ values. - Electronegativity of the group S.¹³ ⁴ Taft's polar substituent constant.^{13b}

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 $\Delta E_{\text{MP}}^{\star}$, as a result of the increased E_{corr}^{\star} relative to E_{corr}^{0} , i.e., $\Delta E_{\text{corr}}^{\star} > 0$.

On the other hand, the HF and MP2 bond distance changes, Δd^* , in Table 4 reveal that within each group, the Δd^* value is smaller for X with a greater electronegativity; the greater the electronegativity of X, the less is the structural reorganization at both the HF and MP2 levels in the activation process. This is also true for the changes in atomic charges; the electronic reorganization or charge transfer is smaller for the X with a greater electronegativity. We therefore conclude that there are two effects of electronegativity of X and/or R: an increase in electronegativity (i) reduces the electronic and structural reorganizations required in the activation process leading to HF ($\Delta E_{\rm HF}^*$) as well as correlated energy barriers (ΔE_{MP}^*), and (ii) increases the electron correlation energy of the TS lowering the ΔE_{MP}^* value only.

As we have noted above, the main structural reorganization involved in the activation process for the identity exchange reactions, equation (1), is the extension of C³-X. The structural changes are determined solely by the requirement to assist charge transfer to the maximum extent.²⁰ According to the principles of the inter-frontier level gap $(\Delta \mathscr{C}_{FMO} = \mathscr{C}_{LUMO} - \mathscr{C}_{HOMO})$ narrowing and frontier electron density growing of Fukui and Fujimoto,²¹ the LUMO, $\sigma^*_{(C-X)}$, is lowered and frontier electron density grows as a reaction proceeds along the reaction coordinate until the TS is reached in order to attain the facile charge transfer required in the TS by providing sufficient charge transfer stabilization, E_{ct} ; a lower σ_{LUMO}^* and a greater frontier electron density lead to a greater charge transfer stabilization energy, E_{ct} , by reducing the inter-frontier level gap, $\Delta \mathscr{C}_{FMO}$, and increasing H_{ii} , respectively, in the equation

$$E_{\rm ct} \approx \frac{H_{ij}^2}{\Delta \mathscr{E}_{\rm FMO}}$$
(2)

Therefore, if σ_{LUMO}^* is low already in the initial state[†] (reactant substrate) due to a strong electronegativity of X and/or R, further assistance required to attain the maximum charge transfer by proceeding along the reaction coordinate, i.e., by expanding the C³-X bond, until the TS is reached can be small, and the TS will be reached by a small extension of C³-X.

Our $HF/6-31++G^{**}//HF/6-31++G^{**}$ level calculations on I and II with Nu = X = H reveal that the effects of R = C₆H₅ in I is similar to those of R = CH₂CH in II; the ΔE^* values are 61.22 kcal mol⁻¹ for I and 63.62 kcal mol⁻¹ for II, and $d^{0}(C^{\alpha}-C^{1}) = 1.5117$ Å contracts by 1.7% and $d^{0}(C-X) = 1.0859$ Å expands by 53.1% in the activation process for I, which compare well with the corresponding changes of -1.4% from $d^{0}(C^{3}-C^{2}) = 1.5025$ Å and +53.7% from $d^{0}(C-X) = 1.0869$ Å for II. The two R groups in fact have very similar group electronegativities (the χ values reported are 5.20 and 4.85 for C₆H₅ and CH₂=CH respectively¹⁴) and Taft's polar substituent constant, σ^{*} (= 0.60 for R = C₆H₅ and 0.56 for R = CH₂CH).^{17b} We therefore think that the allyl system, II, can provide a satisfactory model for the benzyl system, I.

In this respect, the benzylic effect of structure $I^{4.5}$ seems to depend on the electronegativity effect of benzene ring and a smaller extent of bond contraction of the $C^{\alpha}-C^{1}$ bond is in fact more conducive to a rate enhancement, i.e. a lower activation energy, owing to a lesser extent of structural and electronic reorganization required in the TS. This is in contrast to the common conception that a greater benzylic effect is associated with a greater bond contraction of $C^{2}-C^{3}$ in II or $C^{\alpha}-C^{1}$ in I, leading to a greater lowering of the activation energy.

As a result of the π orbital overlap, electronic charge actually flows out of the R group into the C³-X bonds $[\pi_{(R)} \rightarrow \alpha^*_{(C-X)}]$. If the charge were accepted by the R group $[\sigma_{(C-X)} \rightarrow \pi^*_{(R)}]$ resonance delocalization of the C^3 -X orbitals into the π^* orbitals of the R group should result in a greater contraction of the C^3-C^2 bond for a stronger C³-X bond, i.e. a greater decrease in $\Delta d^*(C^3-C^2)$ should result from a smaller increase in $\Delta d^*(C^3-X)$, which is contrary to our findings in Tables 4 and 6. This is especially true for the changes in these bond distances with variation of R (Table 6). The electronegativity of R is greater for CH = C than for $CH_2=CH$, so that we would have expected the extent of resonance electron delocalization to be greater in $CH \equiv CCH_2CI$ if the electronic charge were to flow into the R group from the C^3-X orbitals because of the stronger electronegativity of CH=C. The results (Table 6) are, however, the opposite to this expectation, indicating again that the charge is donated from $\pi_{(R)}$ to $\sigma^*_{(C-X)}$. This is supported by the lower inter-frontier level gaps $\Delta \mathscr{C}_1 = \pi_{(R)} - \sigma^*_{(C-CI)}$ than $\Delta \mathscr{C}_2 = \sigma_{(C-CI)} - \pi^*_{(R)}$ (Table 6), since charge-transfer stabilization, E_{ct} [equation (2)], will be favoured by a smaller energy gap, $\Delta \mathscr{C}_1$, i.e. $\pi_{(R)} - \sigma^*_{(C-X)}$ interaction.

The activation barriers shown in Table 6 demonstrate that even though the methyl transfer reaction (R = H) does not involve any benzylic effect in the TS, the correlated activation barrier, ΔE_{MP}^* , is lower than that

[†] In line with the well known trend of the lower $\sigma^*_{(C-X)}$ LUMO level for a substrate with a more electron-withdrawing (or a more electronegative) substituent (X and/or R), the LUMO $[\sigma^*_{(C-X)}]$ level is successively lowered as the electronegativity of the X and/or R groups increases. the HF $\sigma^*_{(C-X)}$ levels for CH₂CHCH₂X are 0.6188 (X = NH₂), 0.5462 (OH), 0.4633 (F), 0.3822 (PH₂), 0.3649 (SH) and 0.3316 (Cl); for X = Cl, see Table 6.

for the allyl transfer reaction which does involve a benzylic type effect. Steric effects can contribute to the elevation of the activation barrier for the allyl transfer.

Wolfe et al.²² have shown by perturbational molecular orbital (PMO) analyses that the availability of acceptor orbitals on R introduces a stabilizing contribution due to the orbital interactions forming the HOMOs, especiably of type A for TS $(X-CRH_2-X)^-$, where the Xs have non-bonding orbitals. The decreasing $\Delta E_{\rm MP}^*$ values with the increasing acceptor ability as measured by the increasing positive Taft's σ^* constant or by the increasing electronegativity in Table 6 are consistent with the results of such analyses. On the other hand, according to the state correlation diagram (SCD) approach of Shaik *et al.*, 16d,23 the barrier height of an S_{N2} process can be given by a fraction (f) of the energy gap between the ionization potential of the nucleophile (I_{N}) and the electron affinity of the substrate (A_{RX}) , $I_N - A_{RX}$ less the avoided crossing B. This approach predicts that π -acceptor α -carbon substituents such as CH₂CH, CHCH, CN and C₆H₅ improve the substrate acceptor ability markedly without greater delocalizing the C^3-X^- bond. Hence these substituents will enhance reactivity towards powerful nucleophiles. Our results for ΔE_{MP}^* in Table 6 indeed show lower barriers for α -substitution of CHCH and CN. The small barrier height difference $(\Delta \Delta E_{MP}^* = 0.44 \text{ kcal mol}^{-1})$ obtained for substitution of CH₂CH has been ascribed to the opposing effects on f and the energy gap brought about by the α -vinyl group. A similar explanation has been advanced by Shaik et al. for the small reactivity difference due to α -phenyl substitution.



In these two approaches, PMO and SCD, the increased in acceptor ability arising from the α -substitution of R plays an important role in the rate enhancement observed.

SUPPLEMENTARY MATERIALS

Detailed geometries of all structures and energies studied are available.

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